

# Multiscale models

## Coupling spatial models: Autocrine chemotaxis



Cell cluster due to chemotaxis towards self-produced chemoattractant



### Introduction

This example models a cellular Potts model for autocrine chemotaxis by coupling a CPM to a diffusive chemoattractant.

### Model description

It exemplifies the combination of a CPM with a PDE through the chemotaxis towards a diffusive chemoattractant produced by cells. The `CellType` has a Property `p` (production rate) which is positive within biological cells, and is zero in the medium 'cell type'. The symbol `p` can then be used in the PDE as the production term for species or Layer `U`. In this way, `U` is produced in each lattice node that is occupied by a cell, and is not produced outside of cells. At the same time, cells perform Chemotaxis towards the chemoattractant `U`.

The simulation is visualized using some advances Gnuplotter feature. Cells are superimposed on the PDE and appear as transparent domains (see opacity). Moreover, the concentration gradient of the PDE is emphasized by the use of isolines that draws contours as positions with equal concentration.

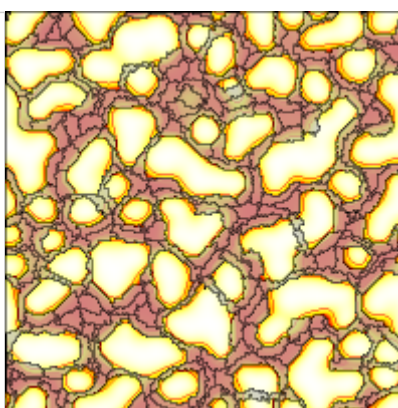
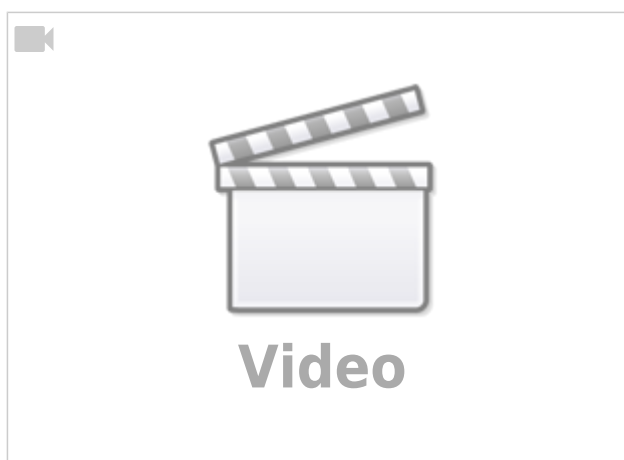
## Model

[h AutocrineChemotaxis.xml |h](#)

```
extern>  
http://imc.zih.tu-dresden.de/morpheus/examples/Multiscale/AutocrineChemotaxis.xml
```

In Morpheus GUI: File → Examples → Multiscale → AutocrineChemotaxis.xml

## Coupling CPM and PDE: Vascular patterning



Cells organize into networks due to matrix-anchorage of chemoattractant

## Introduction

This example shows a model of vascular network formation by paracrine signaling ([Köhn-Luque et al., 2011](#)) and employs a coupled CPM and reaction-diffusion model.

## Model description

The model defines a CPM as well as a PDE. These models are coupled by two processes:

1. Cells, specified in `CellTypes`, respond chemotactically to a Layer (or species) in the PDE
2. Conversely, the production term of one PDE Layer is coupled to the presence/absence of cell.

## Model

[h VascularPatterning.xml |h](#)

```
extern>http://imc.zih.tu-dresden.de/morpheus/examples/Multiscale/VascularPat
```

terning.xml

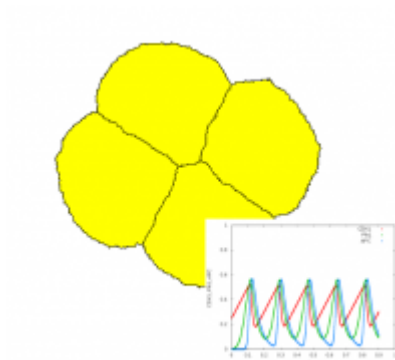
In Morpheus GUI: File → Examples → Multiscale → VascularPatterning.xml

## Reference

Köhn-Luque A, de Back W, Starruß J, Mattiotti A, Deutsch A, et al. [Early Embryonic Vascular Patterning by Matrix-Mediated Paracrine Signalling: A Mathematical Model Study](#). *PLoS ONE* 6(9): e24175, 2011

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## ODEs in CPM cells: Cell cycle and proliferation



Cells divide according to an oscillatory ODE model representing the early cell cycle in *Xenopus*.

## Introduction

This multiscale model example shows

1. how to define a coupled system of continuous ODEs in discrete CPM cells
2. how to specify and change time scales between these model formalisms

## Model description

This model specifies an oscillatory ODE model representing the cell cycle in *Xenopus* oocytes using three components (CDK1, Plk1, APK) (Ferrell et al., *Cell*, 2011) (see `CellTypes→CellType→System`). This ODE model is coupled to 2D shaped CPM cells that perform divide based on the concentration of these components (see `CellTypes→CellType→Proliferation→Condition`). As in the early *Xenopus* cell cleavage, this leads to exponential growth of the number of cells, without increase of total cell volume.

## Time scales

Time scales are defined in the following fashion:

- The so-called global time scheme is defined in `Time` and here runs from 0 to 1 arbitrary time units. All models and plugins specify their updating scheme in terms this global time scheme (e.g. `Analysis→Gnuplotter→interval`).

- The CPM time scale for cell motility and behaviors is defined in `CPM→MCSDuration`. This specifies the time that a single Monte Carlo step in the CPM lasts, in terms of the 'global time'. Here, the `MCSDuration` is  $1.0 \cdot 10^{-4}$  which means the CPM is executed 10.000 times during this simulation.
- For setting time of ODEs, one has to distinguish the (1) how often the ODEs are evaluated from (2) controlling the time scale of the ODE dynamics:
  1. The time scale of the ODE dynamics can be changed using `System→time-scaling` which, when larger or smaller than  $1.0$ , speeds up or slows down make the dynamics, without influencing the accuracy of the approximation.
  2. The accuracy of the numerical approximation (and is equal to the  $\Delta t$  of the numerical solver) is controlled using `System→time-step` (and is automatically rescaled according to the time scale).

## Things to try

- Change the time scale of the CPM relative to the ODE dynamics: Increase `CPM→MCSDuration` to  $1.0 \cdot 10^{-3}$  or decrease to  $1.0 \cdot 10^{-5}$ . This makes cells to have less resp. more motility/relaxation in between cell divisions.
- Change the time scale of the ODE dynamics: Increase `CPM→MCSDuration` to  $1.0 \cdot 10^{-3}$  or decrease to  $1.0 \cdot 10^{-5}$ . This makes cells to have less resp. more motility/relaxation in between cell divisions.

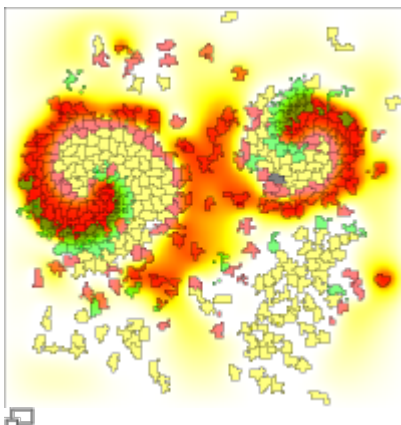
## Model

h [CellCycle.xml](#) |h

```
extern>  
http://imc.zih.tu-dresden.de/morpheus/examples/Multiscale/CellCycle.xml
```

In Morpheus GUI: File → Examples → Multiscale → CellCycle.xml

## Dictyostelium



Aggregation of amoebas through chemotaxis towards waves of cAMP.



## Introduction

This model shows chemotactic aggregation of Dictyostelium. It was constructed by students attending the [ECMI modeling week 2012](#) in Dresden.

## Model description

This model shows an interesting coupling between CPM cells and reaction-diffusion PDE. Cell state depends on the perceived concentration of cAMP, and determines whether a cell produces cAMP and whether it performs chemotaxis. The PDE is governed by a Fitzhugh-Nagumo-like model of an excitable medium, which causes traveling waves upon excitation. Chemotaxis through those waves causes cell aggregation.

Background colors indicate the cAMP concentration. Cells are color-coded according to their phase: excitable/resting (yellow), excited/chemotactic (green), refractory/resting (red).

## Model

h Dictyostelium.xml |h

```
extern>  
http://imc.zih.tu-dresden.de/morpheus/examples/Multiscale/Dictyostelium.xml
```

In Morpheus GUI: File → Examples → Multiscale → Dictyostelium.xml

## References

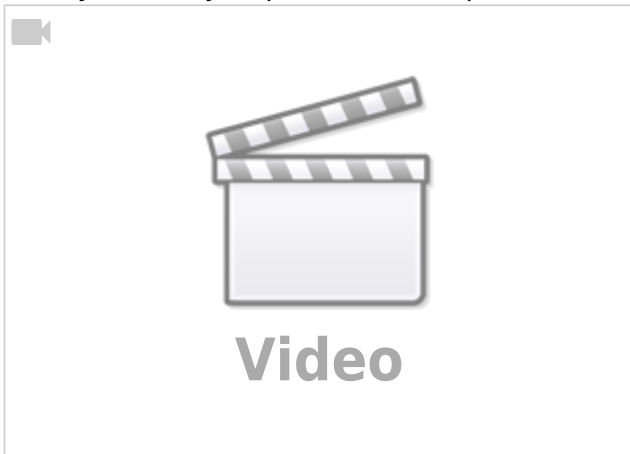
- Savill N and Hogeweg P. [Modelling morphogenesis: from single cells to crawling slugs](#). *J. Theor. Biol.*, 184:229-235, 1997.
- Rost F, Quintero A, Myllykoski M, Igoalkina A, Rohde O'Sullivan Freltoft A, Dixit N, [Morphogenesis and Dynamics of Multicellular Systems](#). *ECMI Newsletter*, 52, 2012.

## MembraneProperties: Cell polarization and chemotaxis

*Note: MembraneProperties are not available in public version of Morpheus.*



Cell dynamically re-polarizes in response to switching external gradient



### Aims

This model show how to couple cells, PDEs on membranes and external gradients.

### Description

This example implements two models of cell polarity: Meinhardt's substrate-depletion model and Edelstein-Keshet's wave-pinning model. The user can switch polarity model by **Disabling/Enabling** the relevant System.

The model defines a one-dimensional reaction-diffusion system (MembraneProperty) representing membrane-bound molecules, and is mapped to a cellular Potts model defining a discrete shaped cell. An external gradient, specified in a PDE, provides a signal for the polarization of the cell. In turn, the polarity of the cell influences its chemotactic behavior.

After a switch in direction of the gradient, the cell re-polarizes in the new direction and starts to move up the gradient, iff the wave pinning model has been selected.

## Model

h CellPolarity.xml |h

```
extern>
```

```
http://imc.zih.tu-dresden.de/morpheus/examples/Multiscale/CellPolarity.xml
```

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Last update: **14:49 30.07.2013**

